



Parallelizing The Laplace Solver





6/4/2012





Writing a parallel program step by step

- Step 1. Start from serial programs as a baseline
 Something to check correctness and efficiency against
- Step 2. Analyze and profile the serial program
 - Identify the "hotspot"
 - Identify the parts that can be parallelized
- Step 3. Parallelize code incrementally
- Step 4. Check correctness of the parallel code
- Step 5. Iterate step 3 and 4











//Read and validate command line arguments

//Initialize the arrays
For each element
value=0

//Set up boundary conditions
For each boundary element
value=something

// Main loop
 For each iteration

 For each element
 Update the value with the 5-point stencil
 Calculate convergence error
 Find maximum convergence error
 If the convergence criterion is met
 Break from the loop

Which parts can and should be parallelized?











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These are the parallelizable parts













What if we have two workers (assuming distributed memory model)?









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We can divide the domain into two parts and assign one to each worker

Anything wrong with this decomposition?





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Each will need their own ghost zone

Independently, They can initialize the array, set the boundary condition and update values using the 5-point stencil.

Is communication necessary?



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After each iteration, they need to exchange boundary data with neighbors. Also, they need to exchange the max convergence error with all other workers so the global error can be found.



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What if we have more workers? Can we still do 1-d decomposition? And does the direction (row or column) of decomposition matter?











1-d decomposition should still work. But how about 2-d decomposition?



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//Read and validate command line arguments

//Initialize the arrays
Decide the array size for each process
For each element
value=0

//Set up boundary conditions
For each boundary element
value=something

// Main loop

For each iteration

For each element

Update the value with the 5-point stencil

Calculate convergence error

Find maximum convergence error

Exchange boundary data with neighbors Exchange the max convergence error with all others

If the convergence criterion is met

Break from the loop

Parallel Laplace solver



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Laplace v0

- 1. MPI_Init etc.
- 2. Calculate subdomain size: $N_{sub} = N/N_{procs}$
- 3. Allocate the array as either $(N_{sub}+2,N+2)$ or $(N+2,N_{sub}+2)$ Laplace v1
- 1. Set boundary condition correctly (using rank and nprocs)
- 2. In each iteration, after updating all element, exchange boundary data:

if (rank != 0) exchange with above or left

- if (rank != nprocs-1) exchange with below or right
- 3. Find the global max convergence error and distribute to all processes

Laplace v2





