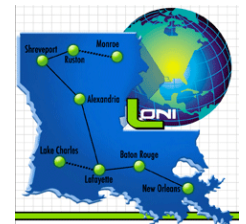


Parallelizing The Laplace Solver

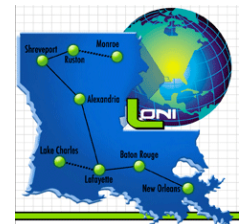


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Writing a parallel program step by step

- Step 1. Start from serial programs as a baseline
 - Something to check correctness and efficiency against
- Step 2. Analyze and profile the serial program
 - Identify the “hotspot”
 - Identify the parts that can be parallelized
- Step 3. Parallelize code incrementally
- Step 4. Check correctness of the parallel code
- Step 5. Iterate step 3 and 4



```
//Read and validate command line arguments
```

```
//Initialize the arrays
For each element
  value=0
```

```
//Set up boundary conditions
For each boundary element
  value=something
```

```
// Main loop
For each iteration
  For each element
    Update the value with the 5-point stencil
    Calculate convergence error
  Find maximum convergence error
  If the convergence criterion is met
    Break from the loop
```

Which parts can and should be parallelized?



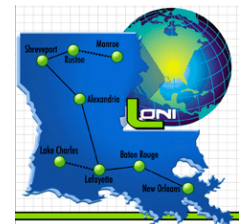
```
//Read and validate command line arguments
```

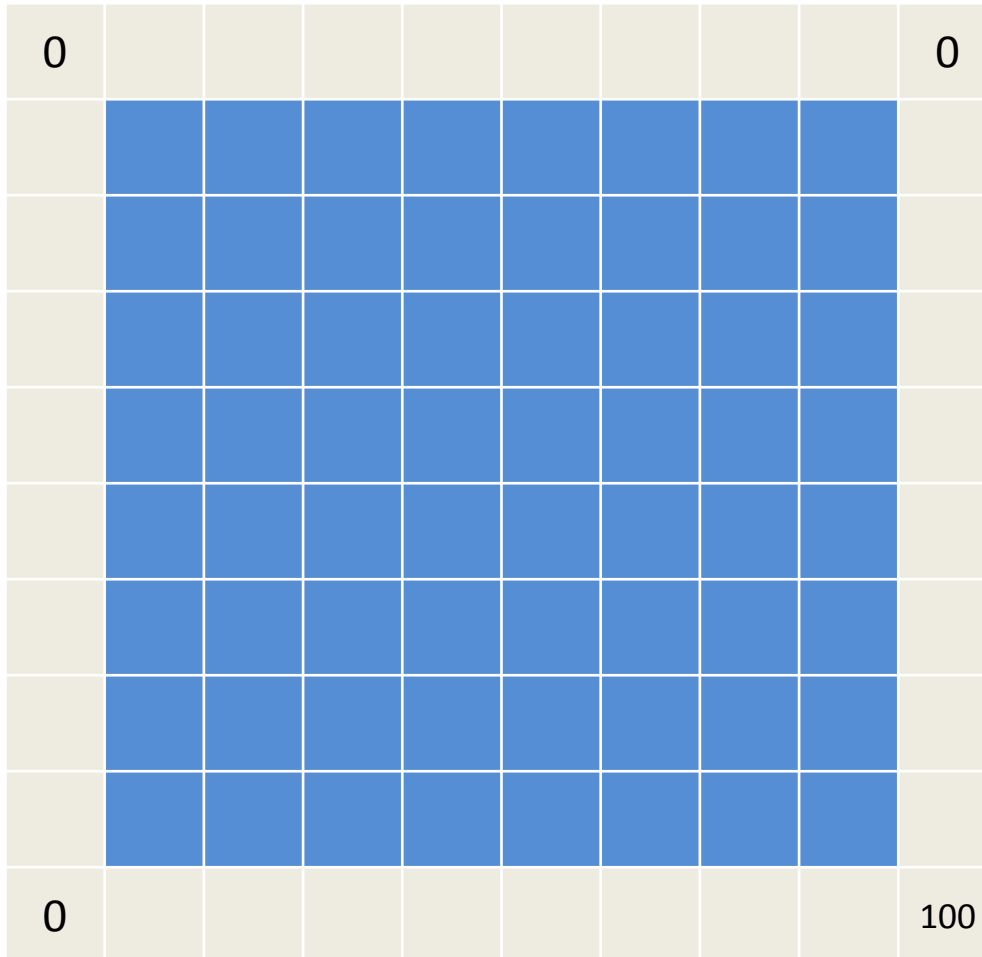
```
//Initialize the arrays
For each element
  value=0
```

```
//Set up boundary conditions
For each boundary element
  value=something
```

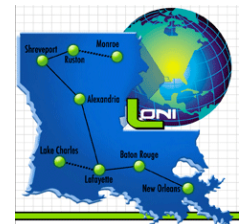
```
// Main loop
For each iteration
  For each element
    Update the value with the 5-point stencil
    Calculate convergence error
  Find maximum convergence error
  If the convergence criterion is met
    Break from the loop
```

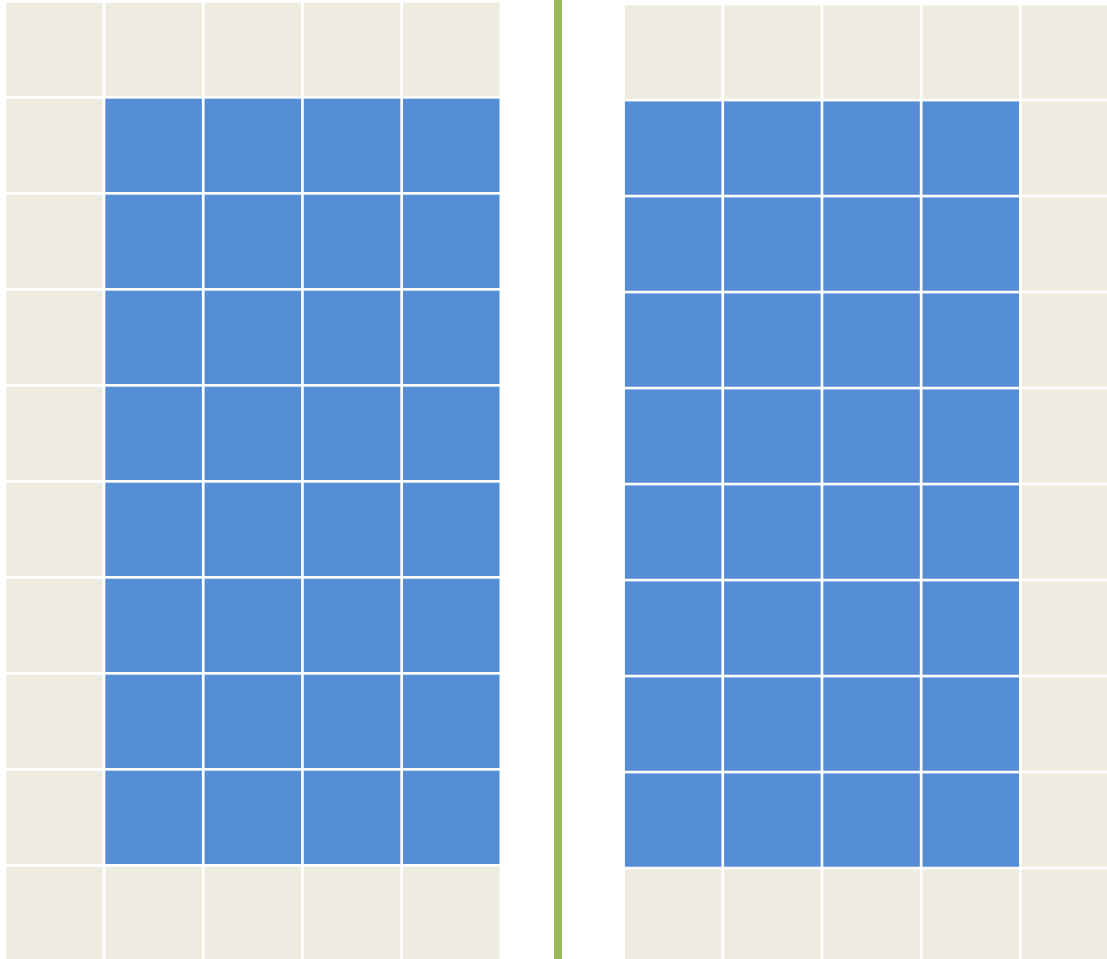
These are the
parallelizable parts





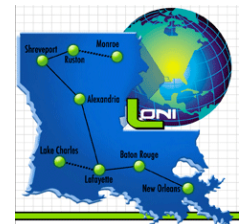
What if we have two workers (assuming distributed memory model)?

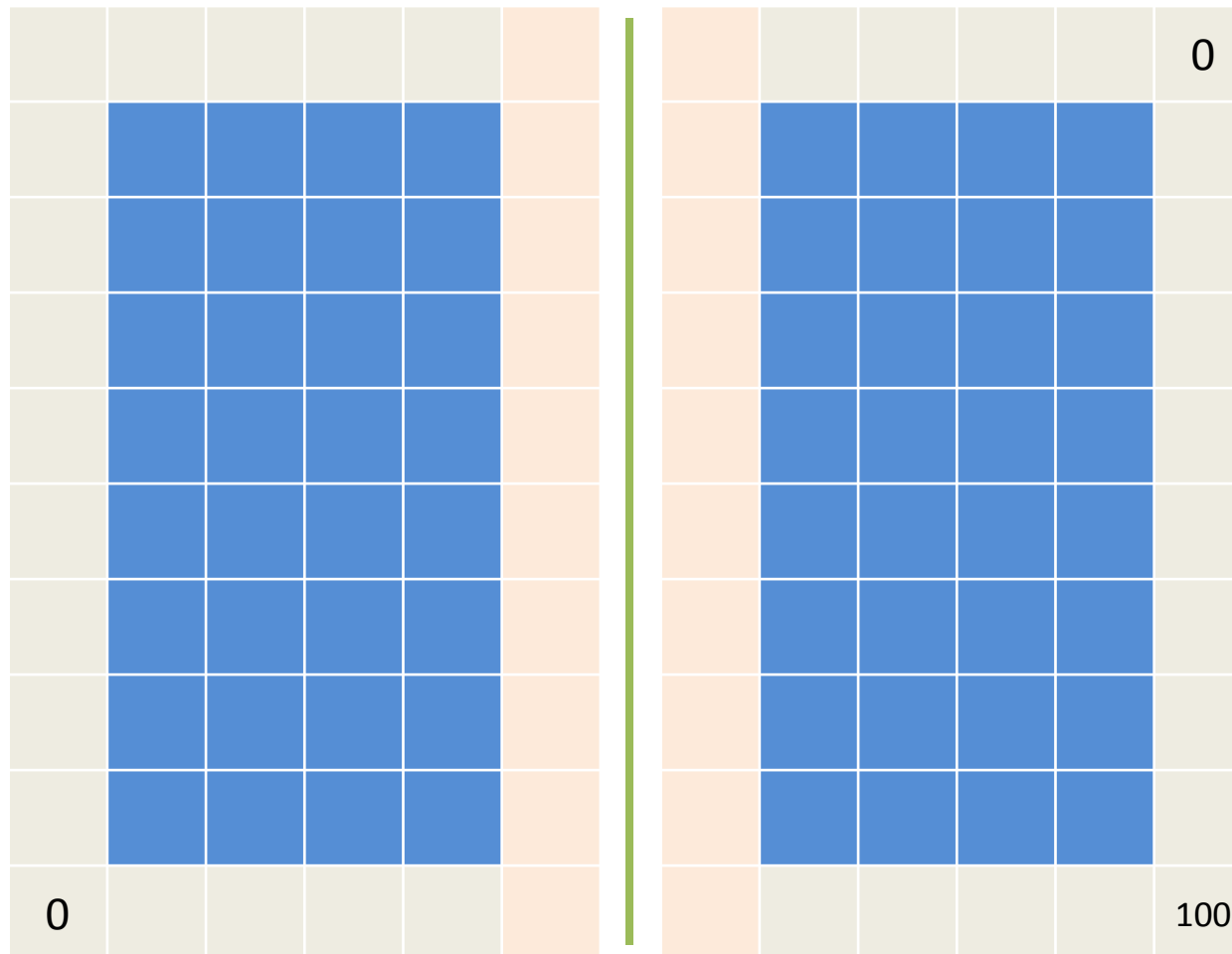




We can divide the domain into two parts and assign one to each worker

Anything wrong with this decomposition?

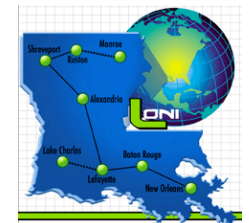


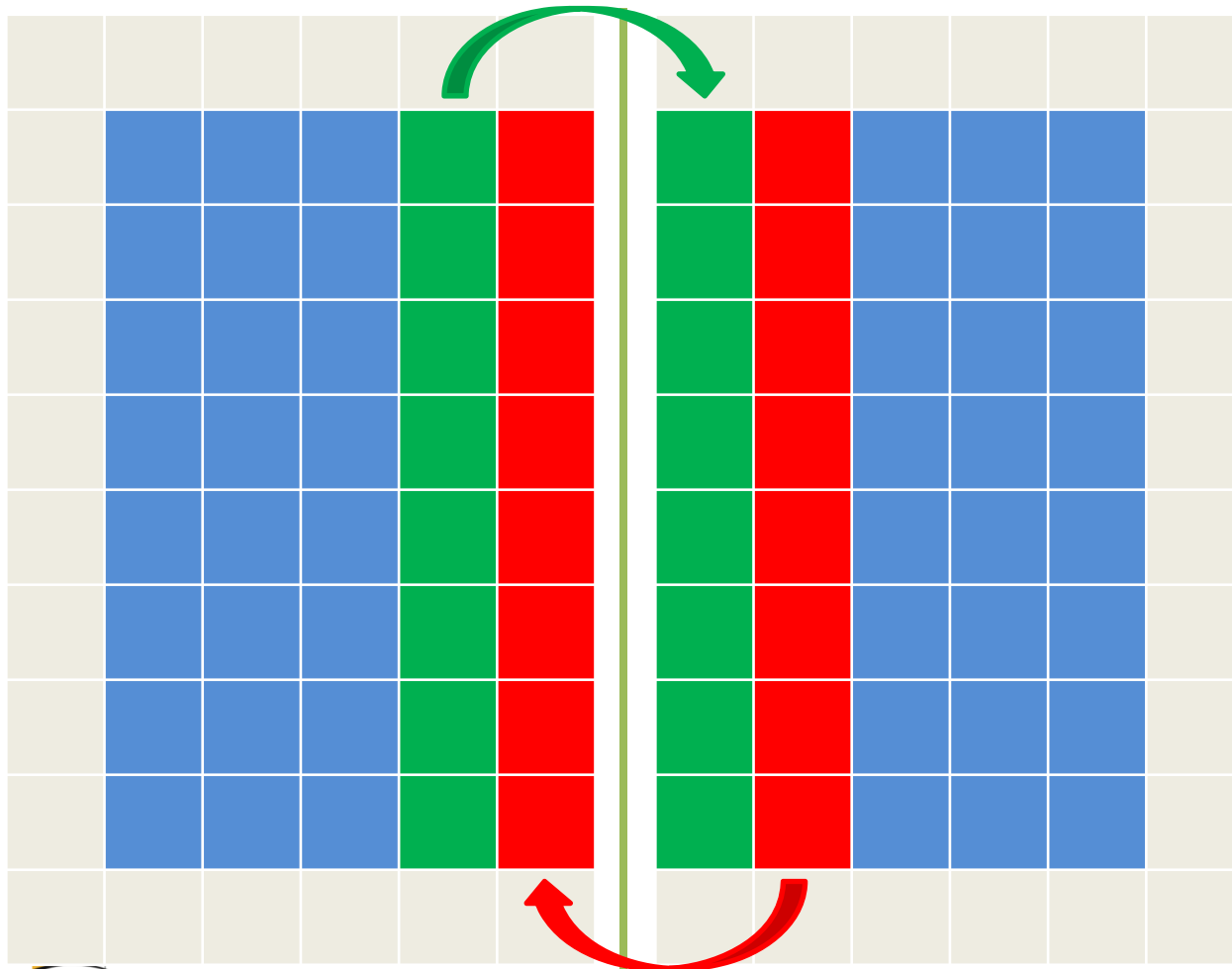


Each will need their own ghost zone

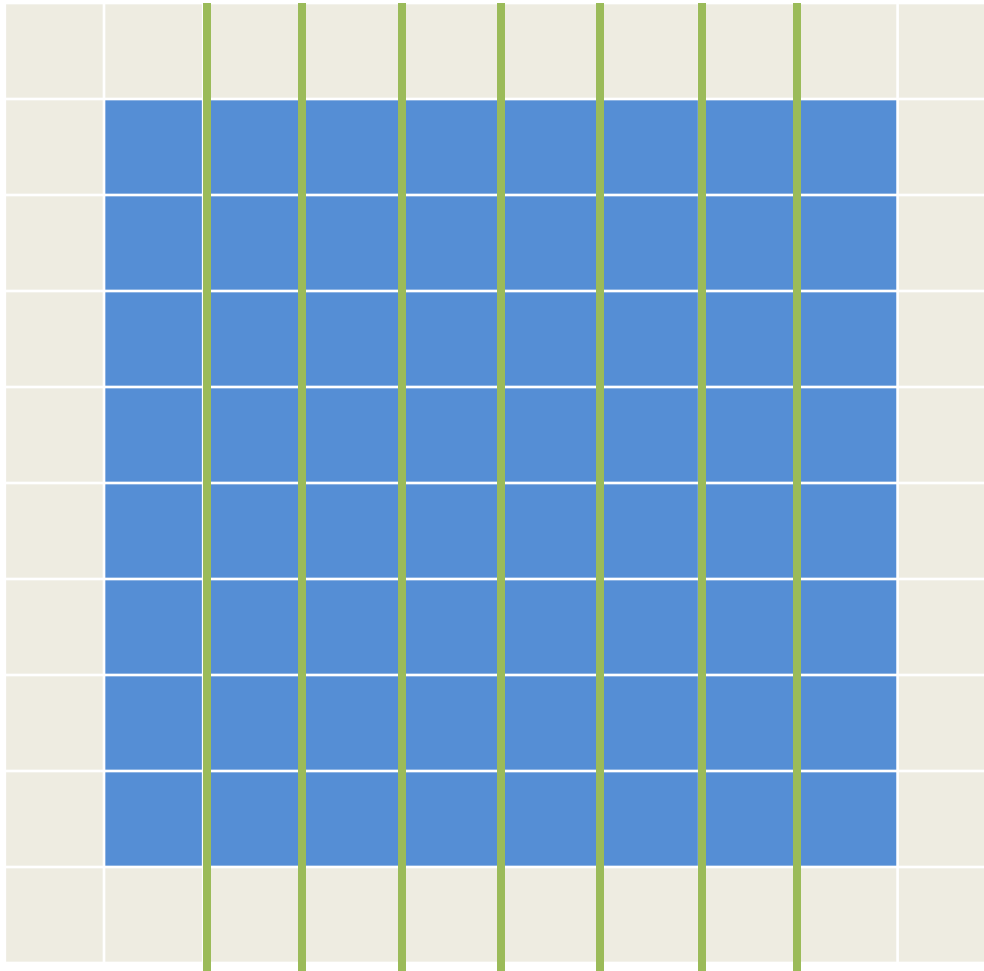
Independently, They can initialize the array, set the boundary condition and update values using the 5-point stencil.

Is communication necessary?

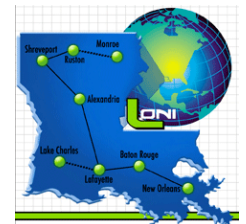


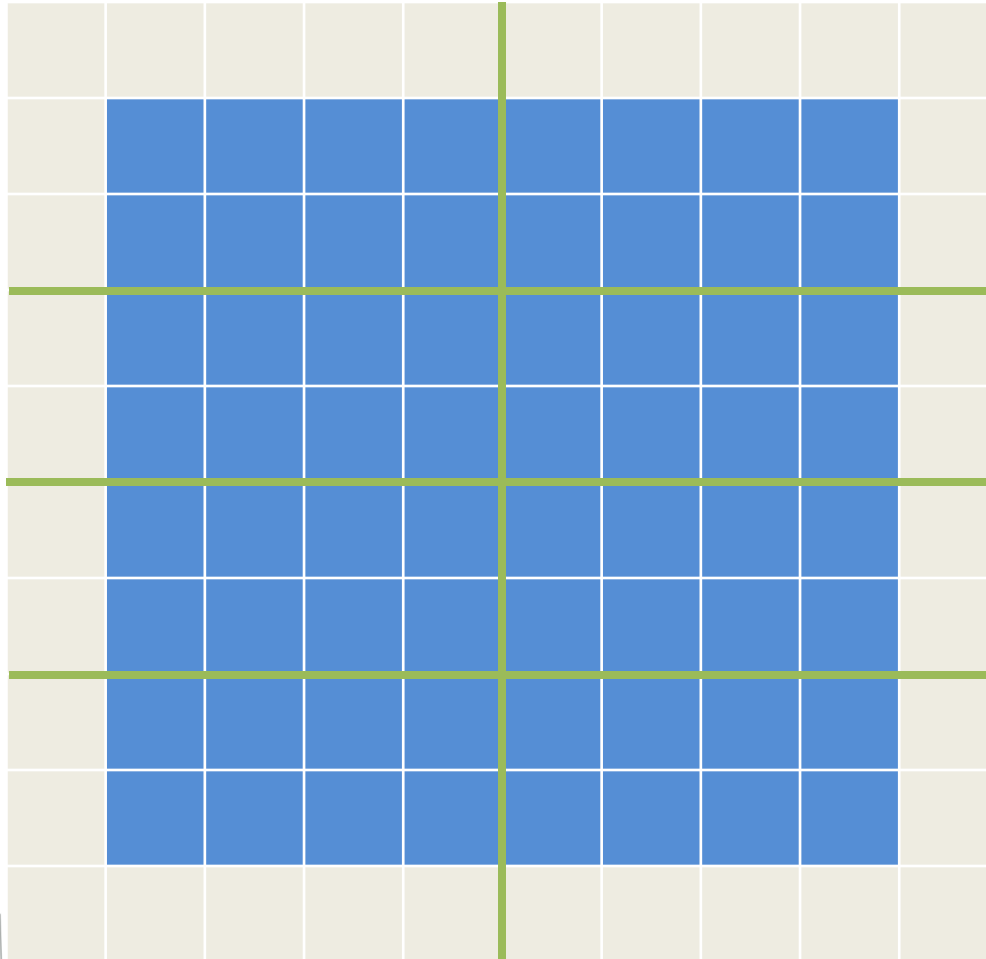


After each iteration, they need to exchange boundary data with neighbors. Also, they need to exchange the max convergence error with all other workers so the global error can be found.



What if we have more workers? Can we still do 1-d decomposition? And does the direction (row or column) of decomposition matter?





1-d decomposition should still work. But how about 2-d decomposition?



```
//Read and validate command line arguments
```

```
//Initialize the arrays
```

```
Decide the array size for each process
```

```
For each element
```

```
value=0
```

```
//Set up boundary conditions
```

```
For each boundary element
```

```
value=something
```

```
// Main loop
```

```
For each iteration
```

```
For each element
```

```
Update the value with the 5-point stencil
```

```
Calculate convergence error
```

```
Find maximum convergence error
```

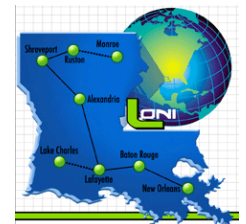
```
Exchange boundary data with neighbors
```

```
Exchange the max convergence error with all others
```

```
If the convergence criterion is met
```

```
Break from the loop
```

Parallel Laplace solver



Laplace v0

1. MPI_Init etc.
2. Calculate subdomain size: $N_{\text{sub}} = N / N_{\text{procs}}$
3. Allocate the array as either $(N_{\text{sub}} + 2, N + 2)$ or $(N + 2, N_{\text{sub}} + 2)$

Laplace v1

1. Set boundary condition correctly (using rank and nprocs)
2. In each iteration, after updating all element, exchange boundary data:
 - if (rank != 0) exchange with above or left
 - if (rank != nprocs-1) exchange with below or right
3. Find the global max convergence error and distribute to all processes

Laplace v2

